

## ***Short Course SC5.14***

# **Practical Ensemble Data Assimilation with the Parallel Data Assimilation Framework**

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<http://pdaf.awi.de>

Hands-on code: <http://pdaf.awi.de/EGU2021>

## The Short Course – Overview

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1. Introduction to ensemble data assimilation
2. Implementation concept of PDAF  
(Parallel Data Assimilation Framework)
3. Hands-on Example:  
A simple assimilation system with PDAF

For hands-on example:  
(try assimilation yourself)

code available at **<http://pdaf.awi.de/EGU2021>**

For hands-on example:  
code available at <http://pdaf.awi.de/EGU2021>

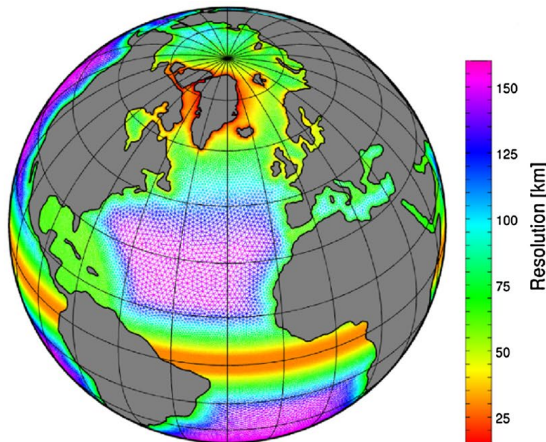
# 1

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## Ensemble Data Assimilation

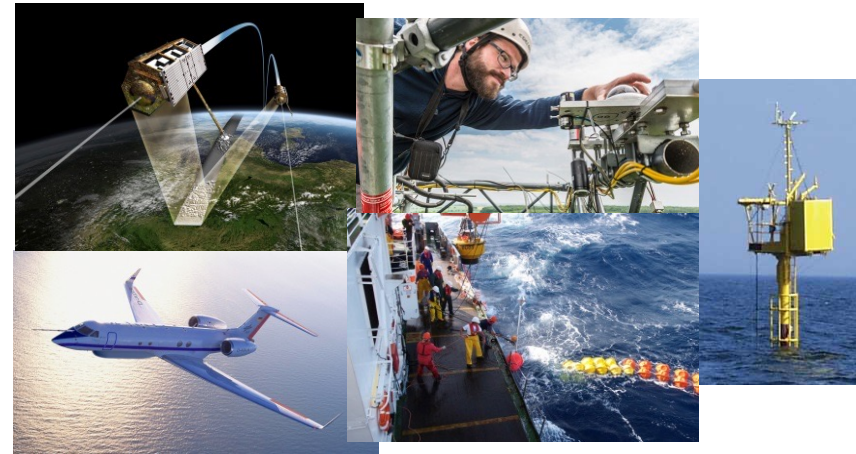
# Data Assimilation

## Models



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## Observations

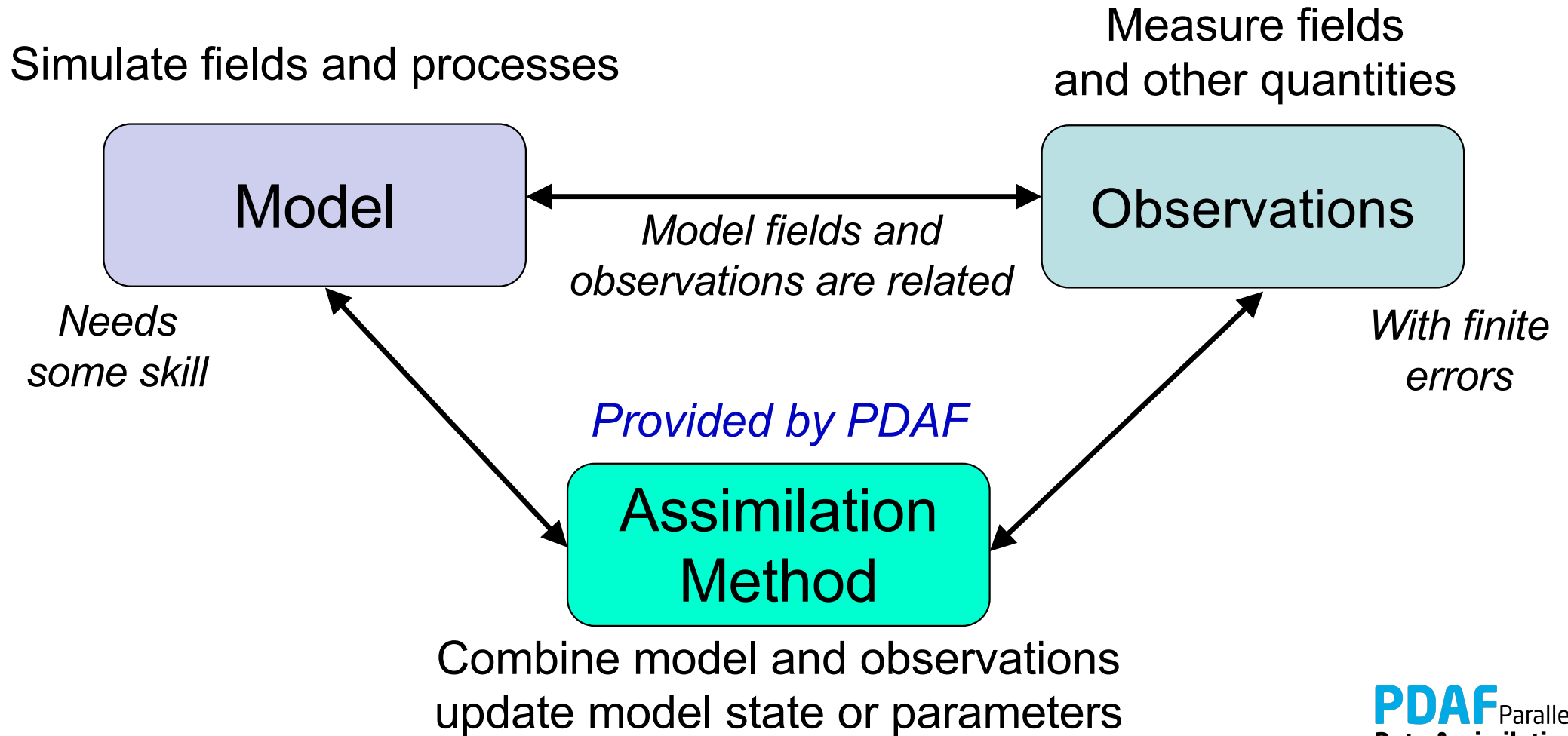


## Data Assimilation

Combine both sources of information quantitatively

- Go beyond just comparing model and observations
- Provide direct link between observations and models
- Allow models to learn from data
- Enhance data products

## Components of an Assimilation System

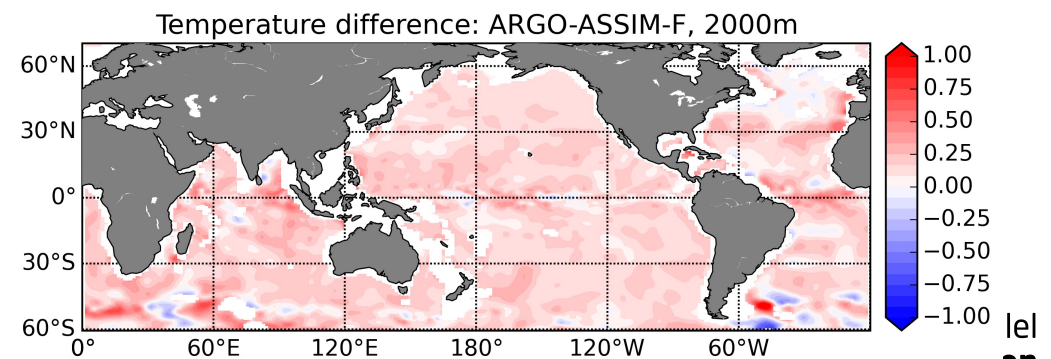
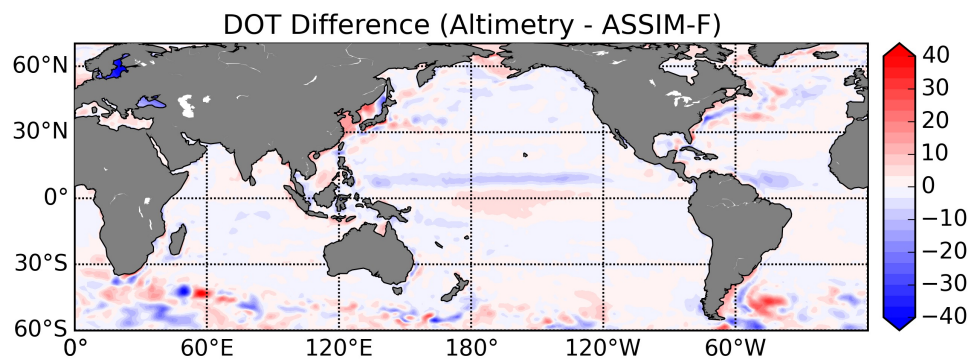
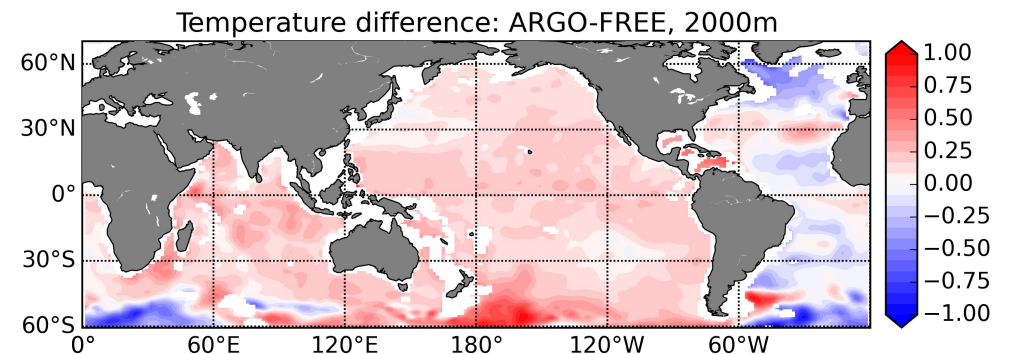
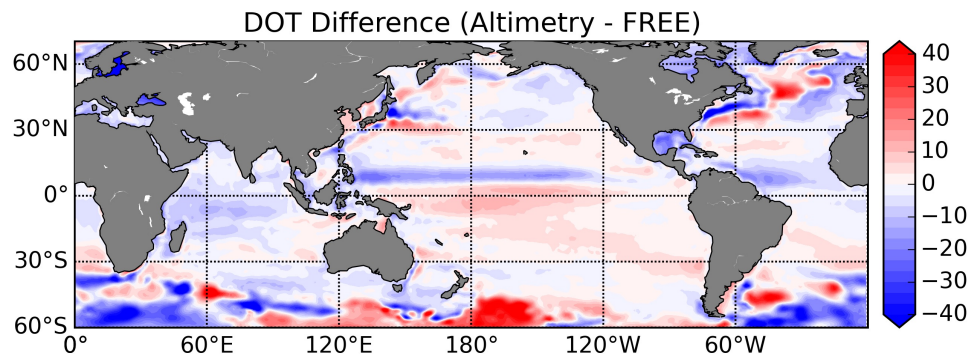


## Example: Assimilation of sea surface height data

**Example:** Assimilate satellite sea surface height data (DOT)

Reduce difference to assimilated  
data (necessary)

Improve also temperature  
at 2000m depth



# Data Assimilation

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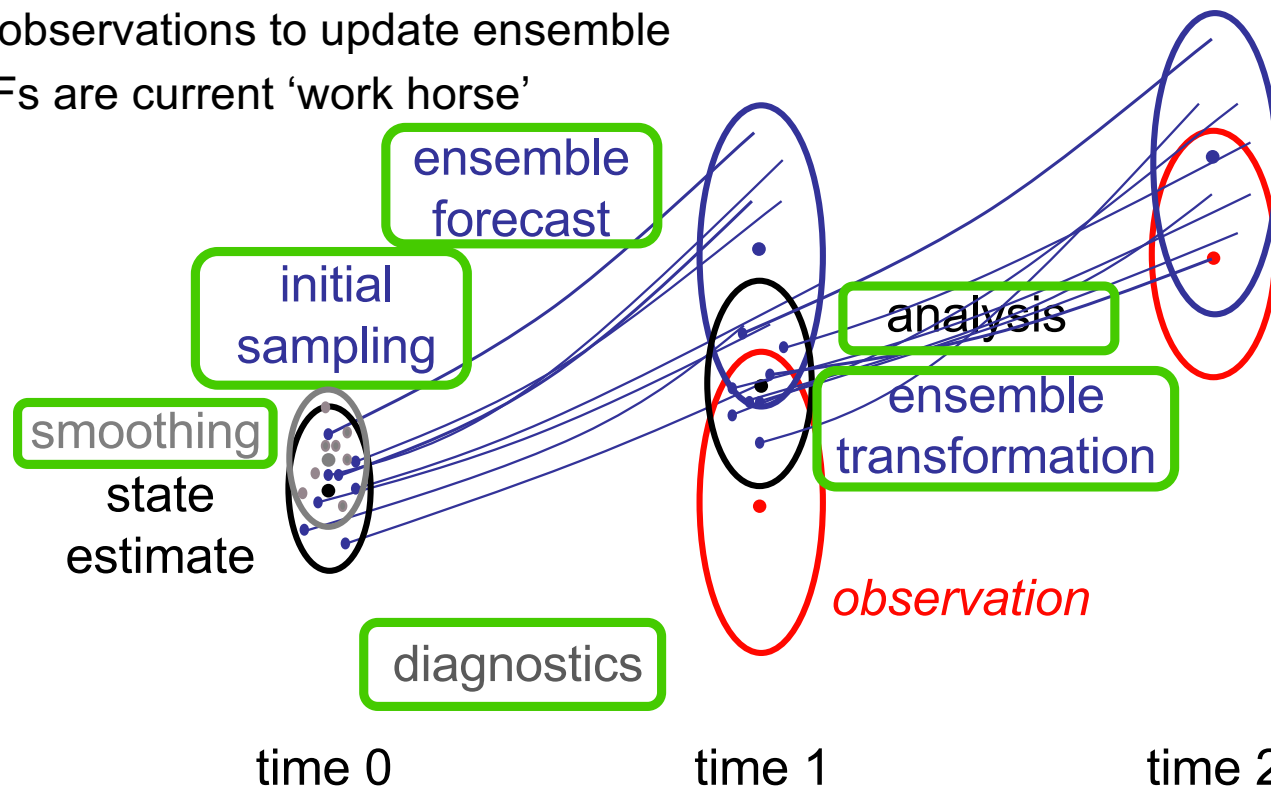
Combine model with real data

- Optimal estimation of system state:
  - initial conditions (for weather/ocean forecasts, ...)
  - state trajectory (temperature, concentrations, ...)
  - parameters (growth of phytoplankton, ice strength, ...)
  - fluxes (heat, primary production, ...)
  - boundary conditions and ‘forcing’ (wind stress, ...)
- More advanced: Improvement of model formulation
  - Detect systematic errors (bias)
  - Revise parameterizations based on parameter estimates

# Ensemble Data Assimilation

## Ensemble Kalman Filters & Particle Filters

- Use ensembles to represent state and uncertainty
- Propagate ensemble using numerical model
- Use observations to update ensemble
- EnKFs are current 'work horse'



These steps can be implemented in a generic way

We can provide software including the algorithms

→ PDAF

**PDAF** Parallel  
Data Assimilation  
Framework



For hands-on example:  
code available at <http://pdaf.awi.de/EGU2021>

## 2

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# Implementation Concept of PDAF (Parallel Data Assimilation Framework)

# PDAF – Community Ensemble Data Assimilation Software

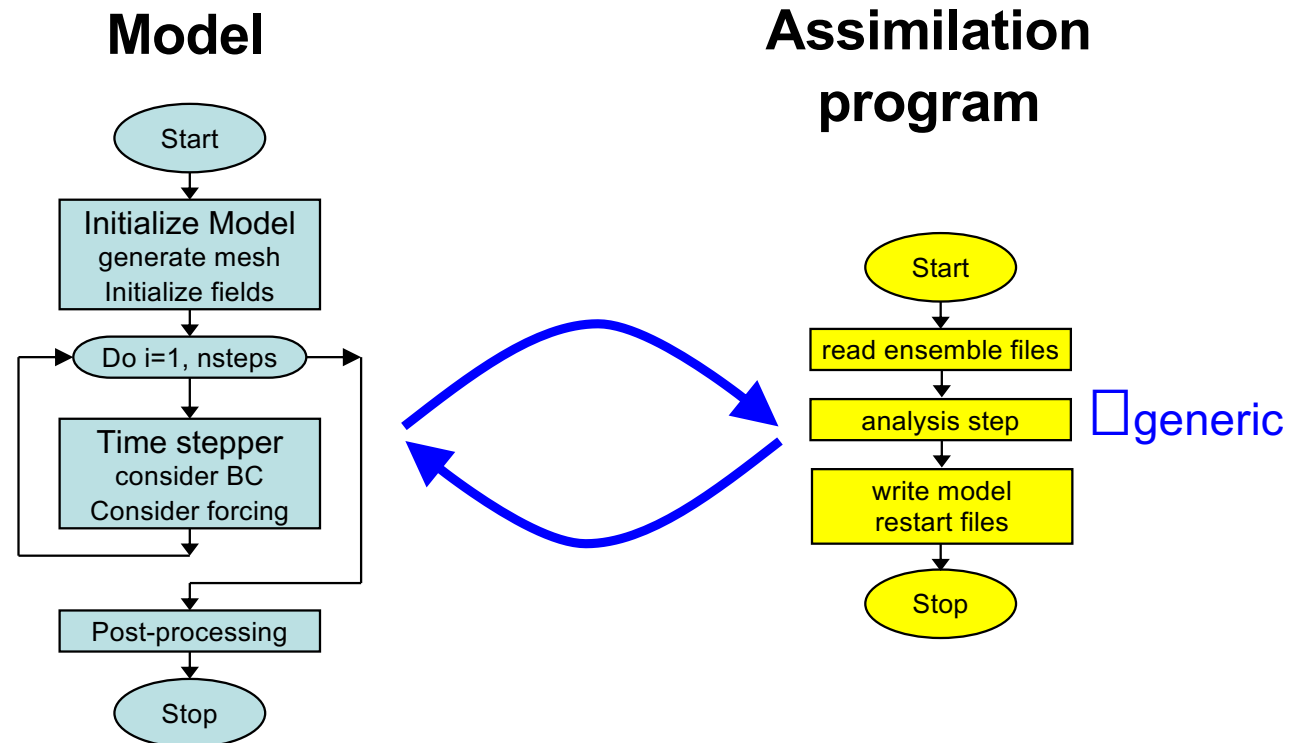
## PDAF - Parallel Data Assimilation Framework

- a program library for ensemble data assimilation
- provides support for parallel ensemble forecasts
- provides filters and smoothers - fully-implemented & parallelized (EnKF, LETKF, LESTKF, NETF, PF ... easy to add more)
- easily usable with (probably) any numerical model (coupled to e.g. NEMO, MITgcm, FESOM, HBM, MPI-ESM, SCHISM/ESMF)
- run from laptops to supercomputers (Fortran, MPI & OpenMP)
- Usable for real assimilation applications and to study assimilation methods
- ~500 registered users; community contributions

Open source:  
Code, documentation, and tutorial available at  
<http://pdaf.awi.de>

## Offline coupling – separate programs

PDAF supports  
offline coupling  
-  
we don't cover  
this here



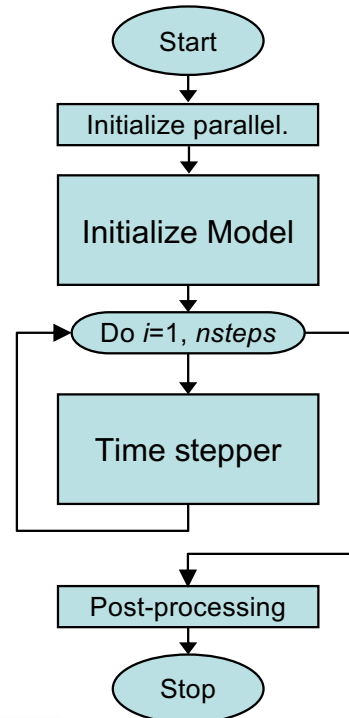
For each ensemble state

- Initialize from restart files
- Integrate
- Write restart files

- Read restart files (ensemble)
- Compute analysis step
- Write new restart files

## Online coupling - Augmenting a Model for Data Assimilation

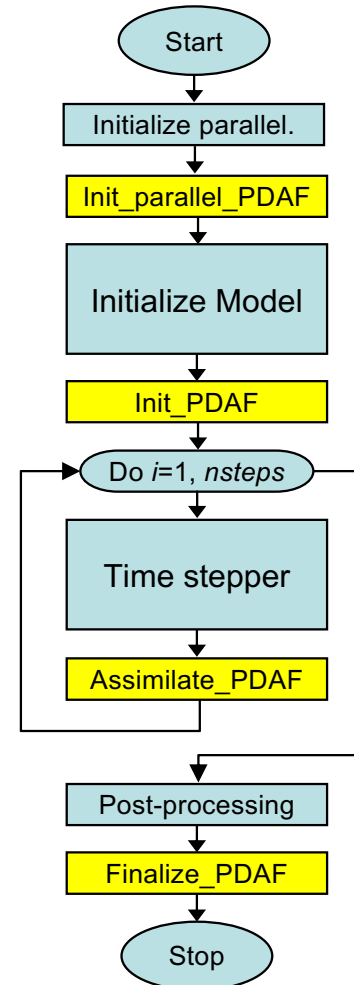
Model



revised parallelization enables ensemble forecast

Data assimilation: run model with additional options

Extension for data assimilation



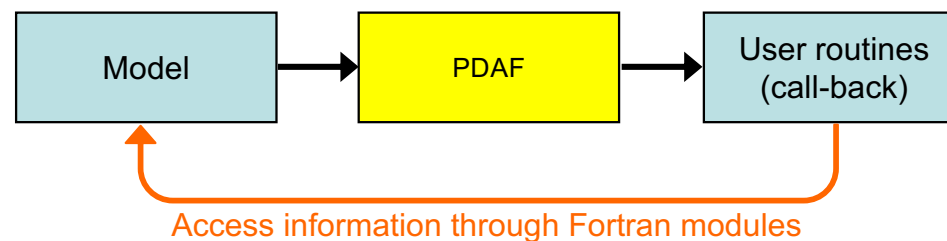
*plus:*  
Possible  
model-specific  
adaption

e.g. in NEMO  
or ECHAM:  
treat leap-frog  
time stepping

**PDAF** Parallel  
Data Assimilation  
Framework

## PDAF interface structure

- Interface routines call PDAF-core routines
- PDAF-core routines call case-specific routines provided by user (included in model binding set)
  - Provide information to PDAF at time when needed
- User-supplied call-back routines for elementary operations:
  - field transformations between model and filter
  - observation-related operations
- User supplied routines can be implemented as routines of the model



SC5.14: Ensemble Data Assimilation with PDAF

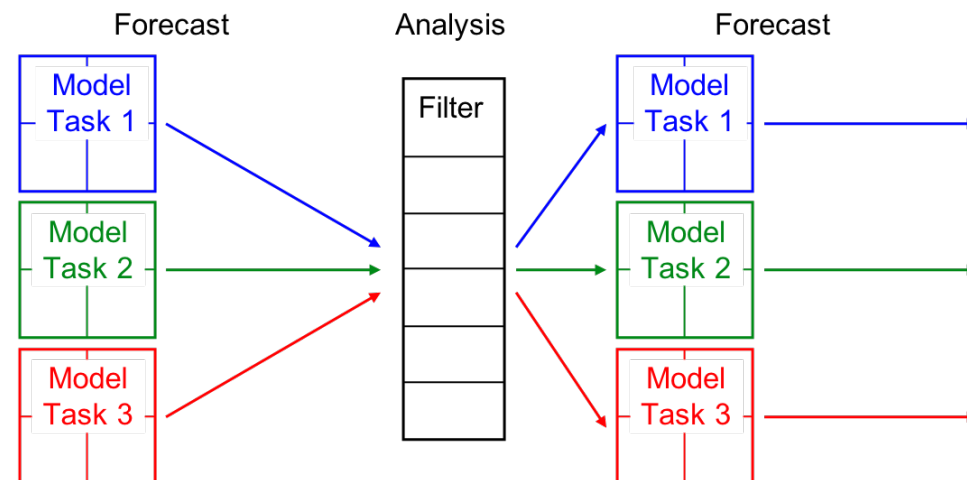
## Modify model to become an 'ensemble model'

We use MPI (Message Passing Interface)

- standard used by most large-scale models

Only need to prepare `init_parallel_pdaf` once for a model

- There is a template that works with most models



Set parameters, for example

- select filter
- set ensemble size

Calls `PDAF_init`

- initialization routine of framework
- provide parameters according to interface
- `PDAF_init` calls the user-provided ensemble initialization routine

## Simple Subroutine Interfaces

Example: ensemble initialization

```
SUBROUTINE init_ens_pdaf(filtertype, dim, dim_ens, state,  
matrU, ens, flag)  
  
    IMPLICIT NONE  
  
    ! ARGUMENTS:  
    INTEGER, INTENT(in) :: filtertype ! Type of filter  
    INTEGER, INTENT(in) :: dim         ! Size of state vector  
    INTEGER, INTENT(in) :: dim_ens    ! Size of ensemble  
    REAL, INTENT(out)  :: ens(dim, dim_ens) ! state ensemble  
    INTEGER, INTENT(inout) :: flag     ! PDAF status flag
```

Task to be implemented:

➤ Fill **ens** with ensemble of initial model states



*calls* PDAF\_assimilate

- checks whether ensemble integration reached time for analysis step
- **If false:**
  - return to model and continue integration
- **If true:**
  - Compute analysis step of chosen filter

Clean-up at end of program (optional)

- Display timing and memory information for PDAF
- Deallocate arrays inside PDAF

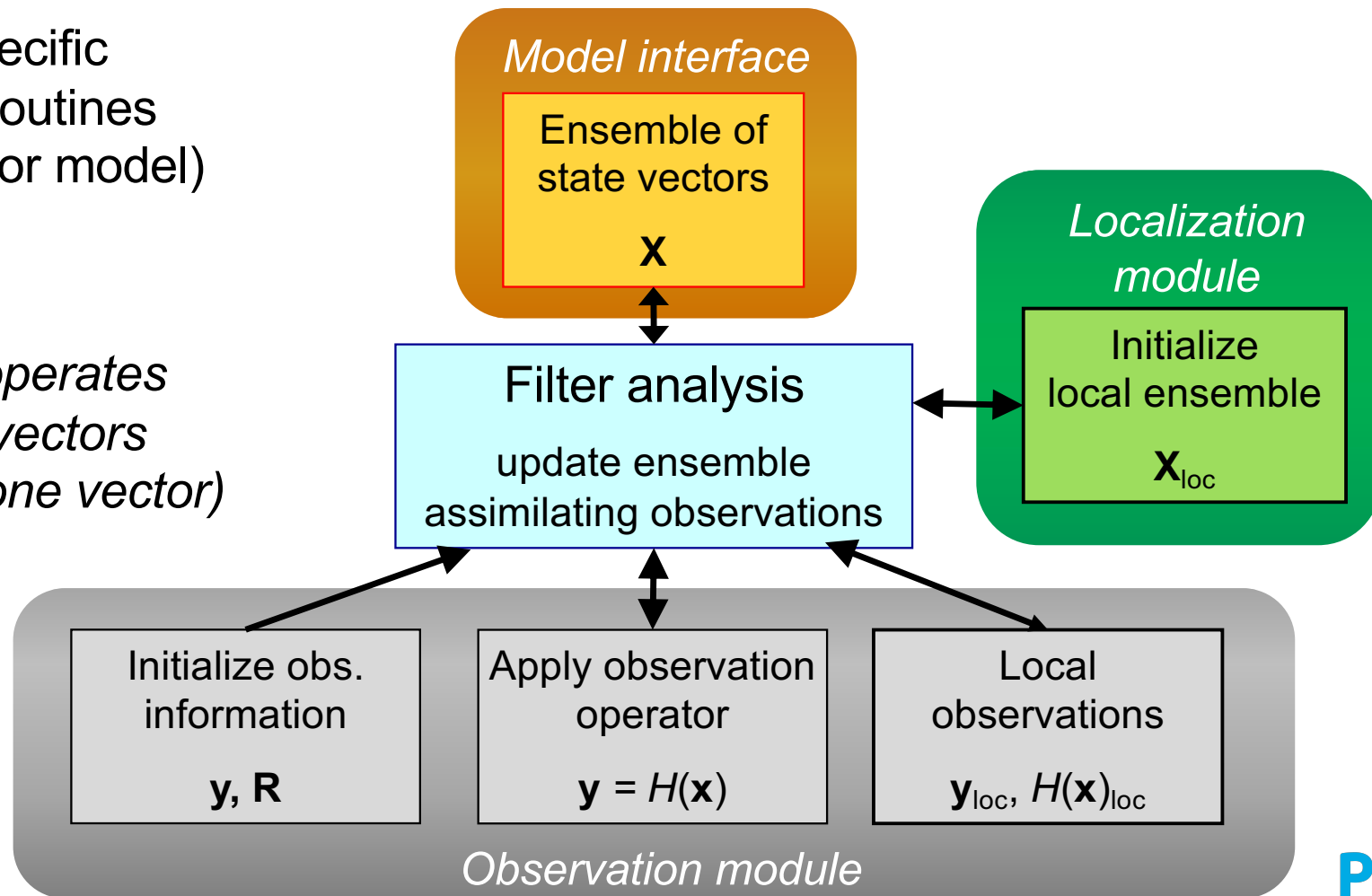
Calls to

PDAF_print_info	(memory and timing info)
PDAF_deallocate	(deallocate arrays)

## Implementing the Ensemble Filter Analysis Step

case-specific  
call-back routines  
(implement for model)

*Analysis operates  
on state vectors  
(all fields in one vector)*



## Implementation concept of PDAF

For ensemble data assimilation with PDAF

- Augment program for ensemble data assimilation (or use separate assimilation program)
- Assimilation methods provided by PDAF
- Model-binding routines required
  - provided MITgcm for test case, and AWI-CM/FESOM
  - easy to code yourself
  - Full implementation for Lorenz96, Lorenz65 and 2d toy model



pdaf@awi.de

Next look into an example

Slides are available online:

<http://pdaf.awi.de>

# 3

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## **Hands-on Example: An Assimilation System built with PDAF**

Tutorial code available at  
<http://pdaf.awi.de/EGU2021>

## Get the tutorial code

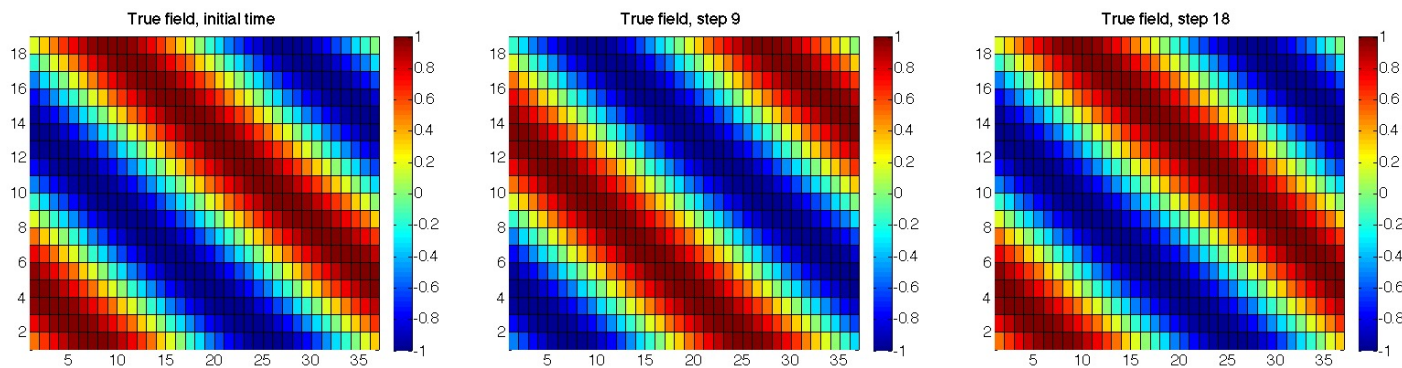
Download the tutorial from <http://pdaf.awi.de/EGU2021>

Directory layout:

<code>make.arch/</code>	- build configurations
<code>src/</code>	- source files
<code>tutorial/</code>	
<code>online_2D_serial/</code>	
<code>model/</code>	- serial model code
<code>model_coupled_to_pdaf/</code>	- final assimilation code
 <code>online_2D_serial.noMPI/</code>	- alternative code without MPI

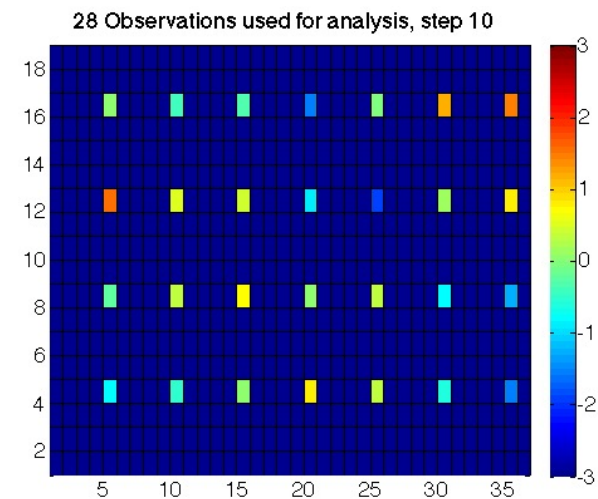
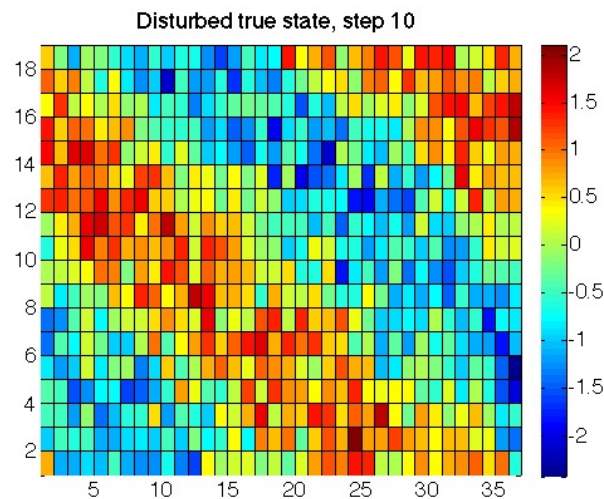
## 2D „Model“

- Simple 2-dimensional grid domain
- 36 x 18 grid points (longitude x latitude)
- True state: sine wave in diagonal direction (periodic for consistent time stepping)
- Simple time stepping:  
Shift field in vertical direction one grid point per time step
- Output to text files (18 rows) – `true_step*.txt`



## Observations

- Add random error to true state (standard deviation 0.5)
- Select a set of observations at 28 grid points
- File storage (in `inputs_online/`):  
text file, full 2D field, -999 marks 'no data' – `obs_step*.txt`  
one file for each time step





## General program structure: model/main.f90

---

```
program main
  initialize
  integrate
end program
```

initialize model information:

- set dimensions
- allocate model field array
- read initial field

perform time stepping

- shift model field
- write new model field

**No parallelization!**

## Files in the tutorial directories

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The model source code consists of the following files (`model/`):

- `main.F90`
- `mod_model.F90`
- `initialize.F90`
- `integrate.F90`
- `Makefile`

## Files in the tutorial directories

The PDAF coupling code consists of (`model_coupled_to_pdaf/`)

- interface subroutines (called from the model code)
  - `init_parallel_pdaf.F90`
  - `init_pdaf.F90`
  - `assimilate_pdaf.F90`
  - `finalize_pdaf.F90`
- user subroutines (called from the PDAF library), eg.
  - `collect_state_pdaf.F90`
- “supporting” modules and subroutines (used in the interface and user subroutines), eg.
  - `mod_assimilation.F90`
  - `init_pdaf_parse.F90`

## Running the tutorial model

- `cd tutorial/online_2D_serialmodel/model`
- Run `make PDAF_ARCH=linux_gfortran`
  - for gcc/gfortran 10 use `linux_gfortran10`
- Run the model with `./model`
- Inputs are read in from `tutorial/inputs_online`
- Outputs are written in `tutorial/online_2D_serialmodel/model`  
eg. `true_step10.txt`
- Plot with python eg.: `../..plotting/plot_file.py true_step18.txt`
- Note: One can also specify `PDAF_ARCH` as environment variable, e.g.  
`export PDAF_ARCH=linux_gfortran`

## Coupling the model to PDAF: Online mode

- Combine model with PDAF into single program
  - `modify Makefile to build model_pdaf`

- Add 4 subroutine calls:

<code>init_parallel_pdaf</code>	- add parallelization
<code>init_pdaf</code>	- initialize assimilation
<code>assimilate_pdaf</code>	- perform assimilation
<code>finalize_pdaf</code>	- clean up

- Implement user subroutines, e.g. for
  - observation operator
  - initialization of observation vector
  - transfer between state vector and model fields

<http://pdaf.awi.de/trac/wiki/OverviewOfUserRoutinesWithDefaultNames>

## Online coupling: Parallelization

- Online coupling avoids writing to disk to exchange state vectors between the model and PDAF
- Add MPI to the model to run several model instances in parallel
- Run the parallel version eg. with

```
mpirun -np 4 ./model_pdaf -dim_ens 4
```

- *Alternative:* PDAF's "flexible" approach:  
<http://pdaf.awi.de/ModifyModelForEnsembleIntegration>
  - `cd to tutorial/online_2D_serialmodel.noMPI/model`

## Adding files for the assimilation – ensemble runs

`init_parallel_pdaf.F90`  
`mod_parallel_pdaf.F90`

} parallelization

`finalize_pdaf.F90`

} clean up

`init_pdaf.F90`  
`mod_assimilation.F90`  
`parser_mpi.F90`  
`init_pdaf_parse.F90`  
`init_ens_pdaf.F90`  
`next_observation_pdaf.F90`  
`distribute_state_pdaf.F90`  
`prepoststep_ens_pdaf.F90`

} initialization

} ensemble forecast

} post step

**PDAF interface subroutine**  
- called from the model  
**helper module/subroutine**  
for the interface  
**PDAF user subroutine** -  
called from PDAF library

Routines are  
generally short –  
PDAF provides  
templates to simplify  
implementation

... (continued on next slide)

Directory: `online_2D_serialmodel/model_coupled_to_pdaf/`

## Adding files for the assimilation – analysis step

... (continued from previous slide)

`assimilate_pdaf.F90`

`collect_state_pdaf.F90`

`callback_obs_pdafomi.F90`

`obs_A_pdafomi.F90`

analysis step

`init_n_domains_pdaf.F90`

`init_dim_1_pdaf.F90`

`g2l_state_pdaf.F90`

`l2g_state_pdaf.F90`

state localization

PDAF interface subroutine  
- called from the model

PDAF user subroutine -  
called from PDAF library

PDAF-OMI observation  
handling - called from  
PDAF library

Routines are  
generally short –  
PDAF provides  
templates to simplify  
implementation

- Each file contains a short summary what the subroutine does
- Templates also describe the required operations



## Modified files in `model_coupled_to_pdaf`

- |                            |  |
|----------------------------|--|
| <code>main.F90</code>      | - added calls to PDAF interface                                    |
| <code>integrate.F90</code> | - added calls to PDAF interface                                    |
| <code>Makefile</code>      | - add linking to PDAF library, PDAF interface and user subroutines |

- Run `make PDAF_ARCH=linux_gfortran_openmpi`
- Then run

```
mpirun -np 5 ./model_pdaf -dim_ens 5
```

- Outputs are written to

```
ens_<i>_step<j>_for.txt
```

```
ens_<i>_step<j>_ana.txt
```

Note: PDAF needs the numerical libraries LAPACK and BLAS (available as standard Linux packages)

This runs a filter without localization with ensemble size 5

## Observation handling – PDAF-OMI

`obs_A_pdafomi.F90` - Observation module containing 3 subroutines:

- `init_dim_obs_A` - initialize observation information
- `obs_op_A` - apply observation operator
- `init_dim_obs_l_A` - find local observations

An observation module contains one observation type

`callback_obs_pdafomi.F90` - Interface routine called by PDAF

- contains the calls to the observation-specific routines
- contains deallocation routine `deallocate_obs_pdafomi`

Other observation types

`obs_B_pdafomi.F90` • Activate with ‘-assim\_B .true.’

`obs_C_pdafomi.F90` • Activate with ‘-assim\_C .true.’

( `obs_C` uses observation operator with interpolation)

## Plotting

- Plotting the results
- With Matlab/Octave you can use

```
load ens_01_step02_for.txt  
pcolor(ens_01_step02_for)
```

- Or use the Python scripts

```
../..plotting/plot_file.py ens_<i>_step<j>_ana.txt  
../..plotting/plot_ens.py <i> <j>
```

(Python plotting requires numpy, matplotlib, and argparse)

## More PDAF experiments

- Find PDAF command line parameters in

```
./model_coupled_to_pdaf/init_pdaf_parse.F90
```

- Try for example

```
mpirun -np 4 ./model_pdaf -dim_ens 4
```

(this runs a filter (ESTKF) without localization with ensemble size 4; it gives a worse result than ensemble size 9)

```
mpirun -np 9 ./model_pdaf -dim_ens 9 -filtertype 7
```

(this runs a filter (LESTKF) with localization and localization radius 0, i.e. correcting only at observed grid points)

```
mpirun -np 9 ./model_pdaf -dim_ens 9 -filtertype 7 -local_range 5
```

(this runs a filter (LESTKF) with localization and localization radius of 5 grid points)

## Current algorithms in PDAF

PDAF originated from comparison studies of different filters

### Filters and smoothers - *global and localized versions*

- EnKF (Evensen, 1994 + perturbed obs.)
- (L)ETKF (Bishop et al., 2001)
- ESTKF (Nerger et al., 2012)
- NETF (Toedter & Ahrens, 2015)
- Particle filter

Not yet released:

- Ensemble 3D-Var
- serial EnSRF
- EWPF

### Model bindings

- MITgcm
- AWI-CM / FESOM

### Toy models

- Lorenz-96 / Lorenz-63

## Feedback, Questions, more code, ...

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Full PDAF package contains

- more tutorial code, more filters
- the fully implemented Lorenz-96/63 models
- MITgcm and FESOM/AWI-CM model bindings

Web site provides an extensive tutorial for self-study

For further questions

- Contact us at [pdaf@awi.de](mailto:pdaf@awi.de)



[pdaf@awi.de](mailto:pdaf@awi.de)

Slides are available online:

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**PDAF** Parallel  
Data Assimilation  
Framework